

# Important Electric Traction Drives Formulas PDF



Formulas  
Examples  
with Units

## List of 13 Important Electric Traction Drives Formulas

### 1) Average Back Emf with Negligible Commutation Overlap Formula

Formula

$$E_b = 1.35 \cdot E_L \cdot \cos(\theta)$$

Example with Units

$$145.6046\text{v} = 1.35 \cdot 120\text{v} \cdot \cos(26^\circ)$$

Evaluate Formula

### 2) DC Output Voltage of Rectifier in Scherbius Drive Given Maximum Rotor Voltage Formula

Formula

$$E_{DC} = 3 \cdot \left( \frac{E_{peak}}{\pi} \right)$$

Example with Units

$$210.0845\text{v} = 3 \cdot \left( \frac{220\text{v}}{3.1416} \right)$$

Evaluate Formula

### 3) DC Output Voltage of Rectifier in Scherbius Drive Given Rotor RMS Line Voltage Formula

Formula

$$E_{DC} = (3 \cdot \sqrt{2}) \cdot \left( \frac{E_r}{\pi} \right)$$

Example with Units

$$210.674\text{v} = (3 \cdot \sqrt{2}) \cdot \left( \frac{156\text{v}}{3.1416} \right)$$

Evaluate Formula

### 4) DC Output Voltage of Rectifier in Scherbius Drive Given Rotor RMS Line Voltage at Slip Formula

Formula

$$E_{DC} = 1.35 \cdot E_{rms}$$

Example with Units

$$210.897\text{v} = 1.35 \cdot 156.22\text{v}$$

Evaluate Formula

### 5) Energy Dissipated during Transient Operation Formula

Formula

$$E_t = \int \left( R \cdot (i)^2, x, 0, T \right)$$

Example with Units

$$160.224\text{J} = \int \left( 4.235\Omega \cdot (2.345\text{A})^2, x, 0, 6.88\text{s} \right)$$

Evaluate Formula



## 6) Equivalent Current for Fluctuating and Intermittent Loads Formula

Formula

Evaluate Formula 

$$I_{eq} = \sqrt{\left(\frac{1}{T}\right) \cdot \int \left( (i)^2, x, 1, T \right)}$$

Example with Units

$$2.1679_A = \sqrt{\left(\frac{1}{6.88_s}\right) \cdot \int \left( (2.345_A)^2, x, 1, 6.88_s \right)}$$

## 7) Gear Tooth Ratio Formula

Formula

Example

Evaluate Formula 

$$a_{gear} = \frac{n_1}{n_2}$$

$$3 = \frac{60}{20}$$

## 8) Motor Terminal Voltage in Regenerative Braking Formula

Formula

Evaluate Formula 

$$V_a = \left(\frac{1}{T}\right) \cdot \int \left( V_s \cdot x, x, t_{on}, T \right)$$

Example with Units

$$385.8454_v = \left(\frac{1}{6.88_s}\right) \cdot \int \left( 118_v \cdot x, x, 1.53_s, 6.88_s \right)$$

## 9) Slip of Scherbius Drive given RMS Line Voltage Formula

Formula

Example with Units

Evaluate Formula 

$$s = \left(\frac{E_b}{E_r}\right) \cdot \text{mod } us(\cos(\theta))$$

$$0.8354 = \left(\frac{145_v}{156_v}\right) \cdot \text{mod } us(\cos(26^\circ))$$

## 10) Starting Time for Induction Motor under No Load Formula

Formula

Evaluate Formula 

$$t_s = \left(-\frac{\tau_m}{2}\right) \cdot \int \left( \left(\frac{s}{s_m} + \frac{s_m}{s}\right) \cdot x, x, 1, 0.05 \right)$$

Example with Units

$$1.2036_s = \left(-\frac{2.359_s}{2}\right) \cdot \int \left( \left(\frac{0.83}{0.67} + \frac{0.67}{0.83}\right) \cdot x, x, 1, 0.05 \right)$$



## 11) Time Taken for Drive Speed Formula ↗

[Evaluate Formula ↗](#)

Formula

$$t = J \cdot \int \left( \frac{1}{\tau - \tau_L}, x, \omega_{m1}, \omega_{m2} \right)$$

Example with Units

$$4.5092 \text{ s} = 10.0 \text{ kg}\cdot\text{m}^2 \cdot \int \left( \frac{1}{5.4 \text{ N}\cdot\text{m} - 0.235 \text{ N}\cdot\text{m}}, x, 2.346 \text{ rad/s}, 4.675 \text{ rad/s} \right)$$

## 12) Torque Generated by Scherbius Drive Formula ↗

[Evaluate Formula ↗](#)

Formula

Example with Units

$$\tau = 1.35 \cdot \left( \frac{E_b \cdot E_L \cdot I_r \cdot E_r}{E_b \cdot \omega_f} \right)$$

$$5.346 \text{ N}\cdot\text{m} = 1.35 \cdot \left( \frac{145 \text{ V} \cdot 120 \text{ V} \cdot 0.11 \text{ A} \cdot 156 \text{ V}}{145 \text{ V} \cdot 520 \text{ rad/s}} \right)$$

## 13) Torque of Squirrel Cage Induction Motor Formula ↗

[Evaluate Formula ↗](#)

Formula

$$\tau = \frac{K \cdot E^2 \cdot R_r}{(R_s + R_r)^2 + (X_s + X_r)^2}$$

Example with Units

$$5.3398 \text{ N}\cdot\text{m} = \frac{0.6 \cdot 200 \text{ V}^2 \cdot 2.75 \Omega}{(55 \Omega + 2.75 \Omega)^2 + (50 \Omega + 45 \Omega)^2}$$



## Variables used in list of Electric Traction Drives Formulas above

- $a_{gear}$  Gear Tooth Ratio
- $E$  Voltage (Volt)
- $E_b$  Back Emf (Volt)
- $E_{DC}$  DC Voltage (Volt)
- $E_L$  AC Line Voltage (Volt)
- $E_{peak}$  Peak Voltage (Volt)
- $E_r$  RMS Value of Rotor Side Line Voltage (Volt)
- $E_{rms}$  Rotor RMS Line Voltage with Slip (Volt)
- $E_t$  Energy Dissipated in Transient Operation (Joule)
- $i$  Electric Current (Ampere)
- $I_{eq}$  Equivalent Current (Ampere)
- $I_r$  Rectified Rotor Current (Ampere)
- $J$  Moment of Inertia (Kilogram Square Meter)
- $K$  Constant
- $n_1$  Number 1 of Teeth of Driving Gear
- $n_2$  Number 2 of Teeth of Driven Gear
- $R$  Resistance of Motor Winding (Ohm)
- $R_r$  Rotor Resistance (Ohm)
- $R_s$  Stator Resistance (Ohm)
- $s$  Slip
- $s_m$  Slip at Maximum Torque
- $t$  Time Taken for Drive Speed (Second)
- $T$  Time Taken for Complete Operation (Second)
- $t_{on}$  On-Period Time (Second)
- $t_s$  Starting Time For Induction motor on No Load (Second)
- $V_a$  Motor Terminal Voltage (Volt)
- $V_s$  Source Voltage (Volt)
- $X_r$  Rotor Reactance (Ohm)
- $X_s$  Stator Reactance (Ohm)
- $\theta$  Firing Angle (Degree)

## Constants, Functions, Measurements used in list of Electric Traction Drives Formulas above

- **constant(s):** pi,  
3.14159265358979323846264338327950288  
*Archimedes' constant*
- **Functions:** cos, cos(Angle)  
*Cosine of an angle is the ratio of the side adjacent to the angle to the hypotenuse of the triangle.*
- **Functions:** int, int(expr, arg, from, to)  
*The definite integral can be used to calculate net signed area, which is the area above the x -axis minus the area below the x -axis.*
- **Functions:** modulus, modulus  
*Modulus of a number is the remainder when that number is divided by another number.*
- **Functions:** sqrt, sqrt(Number)  
*A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.*
- **Measurement:** Time in Second (s)  
*Time Unit Conversion*
- **Measurement:** Electric Current in Ampere (A)  
*Electric Current Unit Conversion*
- **Measurement:** Energy in Joule (J)  
*Energy Unit Conversion*
- **Measurement:** Angle in Degree (°)  
*Angle Unit Conversion*
- **Measurement:** Electric Resistance in Ohm (Ω)  
*Electric Resistance Unit Conversion*
- **Measurement:** Electric Potential in Volt (V)  
*Electric Potential Unit Conversion*
- **Measurement:** Angular Velocity in Radian per Second (rad/s)  
*Angular Velocity Unit Conversion*
- **Measurement:** Torque in Newton Meter (N\*m)  
*Torque Unit Conversion*
- **Measurement:** Moment of Inertia in Kilogram Square Meter (kg·m<sup>2</sup>)  
*Moment of Inertia Unit Conversion*
- **Measurement:** Angular Frequency in Radian per Second (rad/s)



- $T$  Torque (Newton Meter)
- $T_L$  Load Torque (Newton Meter)
- $T_m$  Mechanical Time Constant of Motor (Second)
- $\omega_f$  Angular Frequency (Radian per Second)
- $\omega_{m1}$  Initial Angular Velocity (Radian per Second)
- $\omega_{m2}$  Final Angular Velocity (Radian per Second)

- **Important Electric Traction Drives Formulas** ↗
- **Important Mechanics of Train Movement Formulas** ↗
- **Important Power & Energy Formulas** ↗
- **Important Tractive Effort Formulas** ↗

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