

Important Levelling Formulas PDF



Formulas Examples with Units

List of 23 Important Levelling Formulas

1) Angle of Dip for Compass Surveying Formula ↻

Formula

$$\theta = \frac{D}{R} \cdot \left(\frac{180}{\pi} \right)$$

Example with Units

$$18.2951^\circ = \frac{35.5\text{ m}}{6370} \cdot \left(\frac{180}{3.1416} \right)$$

Evaluate Formula ↻

2) Back Sight given Height of Instrument Formula ↻

Formula

$$BS = HI - RL$$

Example with Units

$$36\text{ m} = 65\text{ m} - 29\text{ m}$$

Evaluate Formula ↻

3) Combined Error Due to Curvature and Refraction Formula ↻

Formula

$$c_r = 0.0673 \cdot D^2$$

Example with Units

$$84.8148\text{ m} = 0.0673 \cdot 35.5\text{ m}^2$$

Evaluate Formula ↻

4) Correction on Refraction Error Formula ↻

Formula

$$c_r = 0.0112 \cdot D^2$$

Example with Units

$$14.1148 = 0.0112 \cdot 35.5\text{ m}^2$$

Evaluate Formula ↻

5) Difference in Elevation between Ground Points in short lines under Trigonometric levelling Formula ↻

Formula

$$\Delta h = D_p \cdot \sin(M) + h_i - h_t$$

Example with Units

$$50.6452\text{ m} = 80\text{ m} \cdot \sin(37^\circ) + 22\text{ m} - 19.5\text{ m}$$

Evaluate Formula ↻

6) Difference in Elevation between Two Points using Barometric Levelling Formula ↻

Formula

$$D_p = 18336.6 \cdot (\log_{10}(h_i) - \log_{10}(h_t)) \cdot \left(1 + \frac{T_1 + T_2}{500} \right)$$

Example with Units

$$2058.2224\text{ m} = 18336.6 \cdot (\log_{10}(22\text{ m}) - \log_{10}(19.5\text{ m})) \cdot \left(1 + \frac{8^\circ\text{C} + 17^\circ\text{C}}{500} \right)$$

Evaluate Formula ↻



7) Distance between Two points under Curvature and Refraction Formula ↻

Formula

$$D = \left(2 \cdot R \cdot c + \left(c^2 \right) \right)^{\frac{1}{2}}$$

Example with Units

$$35.4964\text{ m} = \left(2 \cdot 6370 \cdot 0.0989 + \left(0.0989^2 \right) \right)^{\frac{1}{2}}$$

Evaluate Formula ↻

8) Distance for small errors under Curvature and Refraction Formula ↻

Formula

$$D = \sqrt{2 \cdot R \cdot c}$$

Example with Units

$$35.4963\text{ m} = \sqrt{2 \cdot 6370 \cdot 0.0989}$$

Evaluate Formula ↻

9) Distance to Visible Horizon Formula ↻

Formula

$$D = \sqrt{\frac{h}{0.0673}}$$

Example with Units

$$35.5387\text{ m} = \sqrt{\frac{85\text{ m}}{0.0673}}$$

Evaluate Formula ↻

10) Error Due to Curvature Effect Formula ↻

Formula

$$c = \frac{D^2}{2 \cdot R}$$

Example with Units

$$0.0989 = \frac{35.5\text{ m}^2}{2 \cdot 6370}$$

Evaluate Formula ↻

11) Height of Instrument Formula ↻

Formula

$$HI = RL + BS$$

Example with Units

$$49\text{ m} = 29\text{ m} + 20\text{ m}$$

Evaluate Formula ↻

12) Height of Observer Formula ↻

Formula

$$h = 0.0673 \cdot D^2$$

Example with Units

$$84.8148\text{ m} = 0.0673 \cdot 35.5\text{ m}^2$$

Evaluate Formula ↻

13) Permissible Closing Error for Accurate Levelling Formula ↻

Formula

$$e = 12 \cdot \sqrt{D}$$

Example with Units

$$71.4983\text{ m} = 12 \cdot \sqrt{35.5\text{ m}}$$

Evaluate Formula ↻

14) Permissible Closing Error for Ordinary Levelling Formula ↻

Formula

$$e = 24 \cdot \sqrt{D}$$

Example with Units

$$142.9965\text{ m} = 24 \cdot \sqrt{35.5\text{ m}}$$

Evaluate Formula ↻



15) Permissible Closing Error for Precise Levelling Formula

Formula

$$e = 4 \cdot \sqrt{D}$$

Example with Units

$$23.8328 \text{ m} = 4 \cdot \sqrt{35.5 \text{ m}}$$

Evaluate Formula 

16) Permissible Closing Error for Rough Levelling Formula

Formula

$$e = 100 \cdot \sqrt{D}$$

Example with Units

$$595.8188 \text{ m} = 100 \cdot \sqrt{35.5 \text{ m}}$$

Evaluate Formula 

17) Reduced Level given Height of Instrument Formula

Formula

$$RL = HI - BS$$

Example with Units

$$45 \text{ m} = 65 \text{ m} - 20 \text{ m}$$

Evaluate Formula 

18) Sensitiveness of Level Tube Formulas

18.1) Angle between Line of Sights given Radius of Curvature Formula

Formula

$$\alpha = n \cdot \frac{l}{R_C}$$

Example with Units

$$0.0845 \text{ rad} = 9 \cdot \frac{2 \text{ mm}}{213 \text{ mm}}$$

Evaluate Formula 

18.2) Angle between Line of Sights in Radians Formula

Formula

$$\alpha = \frac{s_i}{D}$$

Example with Units

$$0.0845 \text{ rad} = \frac{3 \text{ m}}{35.5 \text{ m}}$$

Evaluate Formula 

18.3) Distance from Instrument to Staff given Angle between LOS Formula

Formula

$$D = \frac{s_i}{\alpha}$$

Example with Units

$$37.5 \text{ m} = \frac{3 \text{ m}}{0.08 \text{ rad}}$$

Evaluate Formula 

18.4) Number of Division where Bubble Moves given Staff Intercept Formula

Formula

$$n = s_i \cdot \frac{R_C}{l \cdot D}$$

Example with Units

$$9 = 3 \text{ m} \cdot \frac{213 \text{ mm}}{2 \text{ mm} \cdot 35.5 \text{ m}}$$

Evaluate Formula 



18.5) Radius of Curvature of Tube Formula

Formula

$$R_C = n \cdot l \cdot \frac{D}{s_i}$$

Example with Units

$$213_{\text{mm}} = 9 \cdot 2_{\text{mm}} \cdot \frac{35.5_{\text{m}}}{3_{\text{m}}}$$

Evaluate Formula 

18.6) Staff Intercept given Angle between LOS Formula

Formula

$$s_i = \alpha \cdot D$$

Example with Units

$$2.84_{\text{m}} = 0.08_{\text{rad}} \cdot 35.5_{\text{m}}$$

Evaluate Formula 



Variables used in list of Levelling Formulas above

- **BS** Back Sight (*Meter*)
- **c** Error due to Curvature
- **c_r** Refraction Correction
- **c_r** Combined Error (*Meter*)
- **D** Distance between Two Points (*Meter*)
- **D_p** Distance between Points (*Meter*)
- **e** Closing Error (*Meter*)
- **h** Height of Observer (*Meter*)
- **h_i** Height of point A (*Meter*)
- **h_t** Height of point B (*Meter*)
- **HI** Height of Instrument (*Meter*)
- **l** One Division Length (*Millimeter*)
- **M** Measured Angle (*Degree*)
- **n** Number of Division
- **R** Earth Radius in km
- **R_C** Radius of Curvature (*Millimeter*)
- **RL** Reduced Level (*Meter*)
- **s_i** Staff Intercept (*Meter*)
- **T₁** Temperature at Lower Ground Level (*Celsius*)
- **T₂** Temperature at Higher level (*Celsius*)
- **α** Angle between LOS (*Radian*)
- **Δh** Elevation Difference (*Meter*)
- **θ** Dip Angle (*Degree*)

Constants, Functions, Measurements used in list of Levelling Formulas above

- **constant(s):** π ,
3.14159265358979323846264338327950288
Archimedes' constant
- **Functions:** **log10**, $\log_{10}(\text{Number})$
The common logarithm, also known as the base-10 logarithm or the decimal logarithm, is a mathematical function that is the inverse of the exponential function.
- **Functions:** **sin**, $\sin(\text{Angle})$
Sine is a trigonometric function that describes the ratio of the length of the opposite side of a right triangle to the length of the hypotenuse.
- **Functions:** **sqrt**, $\sqrt{\text{Number}}$
A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.
- **Measurement:** **Length** in Meter (m), Millimeter (mm)
Length Unit Conversion 
- **Measurement:** **Temperature** in Celsius (°C)
Temperature Unit Conversion 
- **Measurement:** **Angle** in Degree (°), Radian (rad)
Angle Unit Conversion 



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