

# Important Reactor Performance Equations for Variable Volume Reactions Formulas PDF



**Formulas**  
**Examples**  
**with Units**

## List of 17 Important Reactor Performance Equations for Variable Volume Reactions Formulas

### 1) Initial Reactant Concentration for Second Order Reaction for Mixed Flow Formula

Formula

$$C_{0\text{MixedFlow}} = \left( \frac{1}{\tau_{\text{MFR}} \cdot k''_{\text{MFR}}} \right) \cdot \left( \frac{X_{\text{MFR}} \cdot (1 + (\varepsilon \cdot X_{\text{MFR}}))^2}{(1 - X_{\text{MFR}})^2} \right)$$

Evaluate Formula

Example with Units

$$10.3225 \text{ mol/m}^3 = \left( \frac{1}{0.0612 \text{ s} \cdot 0.0607 \text{ m}^3/(\text{mol}^2\text{s})} \right) \cdot \left( \frac{0.702 \cdot (1 + (0.21 \cdot 0.702))^2}{(1 - 0.702)^2} \right)$$

### 2) Initial Reactant Concentration for Second Order Reaction for Plug Flow Formula

Formula

$$C_{0\text{PlugFlow}} = \left( \frac{1}{\tau_{\text{pfr}} \cdot k''} \right) \cdot \left( 2 \cdot \varepsilon_{\text{PFR}} \cdot (1 + \varepsilon_{\text{PFR}}) \cdot \ln(1 - X_{\text{A-PFR}}) + \varepsilon_{\text{PFR}}^2 \cdot X_{\text{A-PFR}} + \left( (\varepsilon_{\text{PFR}} + 1)^2 \cdot \frac{X_{\text{A-PFR}}}{1 - X_{\text{A-PFR}}} \right) \right)$$

Evaluate Formula

Example with Units

$$1016.2088 \text{ mol/m}^3 = \left( \frac{1}{0.05009 \text{ s} \cdot 0.0608 \text{ m}^3/(\text{mol}^2\text{s})} \right) \cdot \left( 2 \cdot 0.22 \cdot (1 + 0.22) \cdot \ln(1 - 0.715) + 0.22^2 \cdot 0.715 + \left( (0.22 + 1)^2 \cdot \frac{0.715}{1 - 0.715} \right) \right)$$

### 3) Initial Reactant Concentration for Zero Order Reaction for Mixed Flow Formula

Formula

$$C_{0\text{-MFR}} = \frac{k_{0\text{-MFR}} \cdot \tau_{\text{MFR}}}{X_{\text{MFR}}}$$

Example with Units

$$89.0103 \text{ mol/m}^3 = \frac{1021 \text{ mol/m}^3\text{s} \cdot 0.0612 \text{ s}}{0.702}$$

Evaluate Formula

### 4) Initial Reactant Concentration for Zero Order Reaction for Plug Flow Formula

Formula

$$C_{0\text{ pfr}} = \frac{k_0 \cdot \tau_{\text{pfr}}}{X_{\text{A-PFR}}}$$

Example with Units

$$78.4627 \text{ mol/m}^3 = \frac{1120 \text{ mol/m}^3\text{s} \cdot 0.05009 \text{ s}}{0.715}$$

Evaluate Formula

### 5) Rate Constant for First Order Reaction for Mixed Flow Formula

Formula

$$k_{1\text{MFR}} = \left( \frac{1}{\tau_{\text{MFR}}} \right) \cdot \left( \frac{X_{\text{MFR}} \cdot (1 + (\varepsilon \cdot X_{\text{MFR}}))}{1 - X_{\text{MFR}}} \right)$$

Example with Units

$$44.1664 \text{ s}^{-1} = \left( \frac{1}{0.0612 \text{ s}} \right) \cdot \left( \frac{0.702 \cdot (1 + (0.21 \cdot 0.702))}{1 - 0.702} \right)$$

Evaluate Formula



**6) Rate Constant for First Order Reaction for Plug Flow Formula**

Evaluate Formula

Formula

$$k_{\text{plug flow}} = \left( \frac{1}{\tau_{\text{pfr}}} \right) \cdot \left( (1 + \varepsilon_{\text{PFR}}) \cdot \ln \left( \frac{1}{1 - X_{\text{A-PFR}}} \right) - (\varepsilon_{\text{PFR}} \cdot X_{\text{A-PFR}}) \right)$$

Example with Units

$$27.4331 \text{ s}^{-1} = \left( \frac{1}{0.05009 \text{ s}} \right) \cdot \left( (1 + 0.22) \cdot \ln \left( \frac{1}{1 - 0.715} \right) - (0.22 \cdot 0.715) \right)$$

**7) Rate Constant for Second Order Reaction for Mixed Flow Formula**

Evaluate Formula

Formula

$$k^{\text{MixedFlow}} = \left( \frac{1}{\tau_{\text{MFR}} \cdot C_{\text{O-MFR}}} \right) \cdot \left( \frac{X_{\text{MFR}} \cdot (1 + (\varepsilon \cdot X_{\text{MFR}}))^2}{(1 - X_{\text{MFR}})^2} \right)$$

Example with Units

$$13774.7274 \text{ m}^3/(\text{mol} \cdot \text{s}) = \left( \frac{1}{0.0612 \text{ s}} \cdot 81 \text{ mol/m}^3 \right) \cdot \left( \frac{0.702 \cdot (1 + (0.21 \cdot 0.702))^2}{(1 - 0.702)^2} \right)$$

**8) Rate Constant for Second Order Reaction for Plug Flow Formula**

Evaluate Formula

Formula

$$k^{\text{PlugFlow}} = \left( \frac{1}{\tau \cdot C_0} \right) \cdot \left( 2 \cdot \varepsilon \cdot (1 + \varepsilon) \cdot \ln(1 - X_{\text{A}}) + \varepsilon^2 \cdot X_{\text{A}} + \left( (\varepsilon + 1)^2 \cdot \frac{X_{\text{A}}}{1 - X_{\text{A}}} \right) \right)$$

Example with Units

$$0.7088 \text{ m}^3/(\text{mol} \cdot \text{s}) = \left( \frac{1}{0.05 \text{ s} \cdot 80 \text{ mol/m}^3} \right) \cdot \left( 2 \cdot 0.21 \cdot (1 + 0.21) \cdot \ln(1 - 0.7) + 0.21^2 \cdot 0.7 + \left( (0.21 + 1)^2 \cdot \frac{0.7}{1 - 0.7} \right) \right)$$

**9) Rate Constant for Zero Order Reaction for Mixed Flow Formula**

Evaluate Formula

Formula

$$k_{\text{O-MFR}} = \frac{X_{\text{MFR}} \cdot C_{\text{O-MFR}}}{\tau_{\text{MFR}}}$$

Example with Units

$$929.1176 \text{ mol/m}^3 \cdot \text{s} = \frac{0.702 \cdot 81 \text{ mol/m}^3}{0.0612 \text{ s}}$$

**10) Rate Constant for Zero Order Reaction for Plug Flow Formula**

Evaluate Formula

Formula

$$k_0 = \frac{X_{\text{A-PFR}} \cdot C_{\text{O pfr}}}{\tau_{\text{pfr}}}$$

Example with Units

$$1170.4931 \text{ mol/m}^3 \cdot \text{s} = \frac{0.715 \cdot 82 \text{ mol/m}^3}{0.05009 \text{ s}}$$

**11) Reactant Conversion for Zero Order Reaction for Mixed Flow Formula**

Evaluate Formula

Formula

$$X_{\text{MFR}} = \frac{k_{\text{O-MFR}} \cdot \tau_{\text{MFR}}}{C_{\text{O-MFR}}}$$

Example with Units

$$0.7714 = \frac{1021 \text{ mol/m}^3 \cdot \text{s} \cdot 0.0612 \text{ s}}{81 \text{ mol/m}^3}$$

**12) Reactant Conversion for Zero Order Reaction for Plug Flow Formula**

Evaluate Formula

Formula

$$X_{\text{A-PFR}} = \frac{k_0 \cdot \tau_{\text{pfr}}}{C_{\text{O pfr}}}$$

Example with Units

$$0.6842 = \frac{1120 \text{ mol/m}^3 \cdot \text{s} \cdot 0.05009 \text{ s}}{82 \text{ mol/m}^3}$$



**13) Space Time for First Order Reaction using Rate Constant for Mixed Flow Formula**

Formula

$$\tau_{MFR} = \left( \frac{1}{k_{1MFR}} \right) \cdot \left( \frac{X_{MFR} \cdot (1 + (\varepsilon \cdot X_{MFR}))}{1 - X_{MFR}} \right)$$

Example with Units

$$0.0683 \text{ s} = \left( \frac{1}{39.6 \text{ s}^{-1}} \right) \cdot \left( \frac{0.702 \cdot (1 + (0.21 \cdot 0.702))}{1 - 0.702} \right)$$

Evaluate Formula

**14) Space Time for First Order Reaction using Rate Constant for Plug Flow Formula**

Formula

$$\tau_{pfr} = \left( \frac{1}{k_{plug \text{ flow}}} \right) \cdot \left( (1 + \varepsilon_{PFR}) \cdot \ln \left( \frac{1}{1 - X_{A-PFR}} \right) - (\varepsilon_{PFR} \cdot X_{A-PFR}) \right)$$

Example with Units

$$0.0348 \text{ s} = \left( \frac{1}{39.5 \text{ s}^{-1}} \right) \cdot \left( (1 + 0.22) \cdot \ln \left( \frac{1}{1 - 0.715} \right) - (0.22 \cdot 0.715) \right)$$

Evaluate Formula

**15) Space Time for Second Order Reaction using Rate Constant for Mixed Flow Formula**

Formula

$$\tau_{MixedFlow} = \left( \frac{1}{k''_{MFR} \cdot C_{o-MFR}} \right) \cdot \left( \frac{X_{MFR} \cdot (1 + (\varepsilon \cdot X_{MFR}))^2}{(1 - X_{MFR})^2} \right)$$

Example with Units

$$13888.193 \text{ s} = \left( \frac{1}{0.0607 \text{ m}^3/(\text{mol} \cdot \text{s})} \cdot 81 \text{ mol/m}^3 \right) \cdot \left( \frac{0.702 \cdot (1 + (0.21 \cdot 0.702))^2}{(1 - 0.702)^2} \right)$$

Evaluate Formula

**16) Space Time for Zero Order Reaction using Rate Constant for Mixed Flow Formula**

Formula

$$\tau_{MFR} = \frac{X_{MFR} \cdot C_{o-MFR}}{k_{0-MFR}}$$

Example with Units

$$0.0557 \text{ s} = \frac{0.702 \cdot 81 \text{ mol/m}^3}{1021 \text{ mol/m}^3 \cdot \text{s}}$$

Evaluate Formula

**17) Space Time for Zero Order Reaction using Rate Constant for Plug Flow Formula**

Formula

$$\tau_{pfr} = \frac{X_{A-PFR} \cdot C_{o \text{ pfr}}}{k_0}$$

Example with Units

$$0.0523 \text{ s} = \frac{0.715 \cdot 82 \text{ mol/m}^3}{1120 \text{ mol/m}^3 \cdot \text{s}}$$

Evaluate Formula



## Variables used in list of Reactor Performance Equations for Variable Volume Reactions Formulas above

- $C_{o\ pfr}$  Initial Reactant Concentration in PFR (Mole per Cubic Meter)
- $C_o$  Initial Reactant Concentration (Mole per Cubic Meter)
- $C_{o-MFR}$  Initial Reactant Concentration in MFR (Mole per Cubic Meter)
- $C_{oMixedFlow}$  Initial Reactant Conc for 2nd Order Mixed Flow (Mole per Cubic Meter)
- $C_{oPlugFlow}$  Initial Reactant Conc for 2nd Order Plug Flow (Mole per Cubic Meter)
- $k_0$  Rate Constant for Zero Order Reaction (Mole per Cubic Meter Second)
- $k_{0-MFR}$  Rate Constant for Zero Order Reaction in MFR (Mole per Cubic Meter Second)
- $k_{plug\ flow}$  Rate Constant for First Order in Plug Flow (1 Per Second)
- $k''_{MFR}$  Rate Constant for Second Order Reaction in MFR (Cubic Meter per Mole Second)
- $k''$  Rate Constant for Second Order Reaction (Cubic Meter per Mole Second)
- $k_{MixedFlow''}$  Rate Constant for 2nd Order Reaction for Mixed Flow (Cubic Meter per Mole Second)
- $k_{PlugFlow''}$  Rate Constant for 2nd Order Reaction for Plug Flow (Cubic Meter per Mole Second)
- $k_{1MFR}$  Rate Constant for First Order Reaction in MFR (1 Per Second)
- $X_A$  Reactant Conversion
- $X_{A-PFR}$  Reactant Conversion in PFR
- $X_{MFR}$  Reactant Conversion in MFR
- $\epsilon$  Fractional Volume Change in Reactor
- $\epsilon$  Fractional Volume Change
- $\epsilon_{PFR}$  Fractional Volume Change in PFR
- $\tau$  Space Time (Second)
- $\tau_{MFR}$  Space Time in MFR (Second)
- $\tau_{MixedFlow}$  Space Time for Mixed Flow (Second)
- $\tau_{pfr}$  Space Time in PFR (Second)

## Constants, Functions, Measurements used in list of Reactor Performance Equations for Variable Volume Reactions Formulas above

- **Functions:**  $\ln$ ,  $\ln(\text{Number})$   
The natural logarithm, also known as the logarithm to the base  $e$ , is the inverse function of the natural exponential function.
- **Measurement:** **Time** in Second (s)  
Time Unit Conversion 
- **Measurement:** **Molar Concentration** in Mole per Cubic Meter ( $\text{mol}/\text{m}^3$ )  
Molar Concentration Unit Conversion 
- **Measurement:** **Reaction Rate** in Mole per Cubic Meter Second ( $\text{mol}/\text{m}^3\cdot\text{s}$ )  
Reaction Rate Unit Conversion 
- **Measurement:** **First Order Reaction Rate Constant** in 1 Per Second ( $\text{s}^{-1}$ )  
First Order Reaction Rate Constant Unit Conversion 
- **Measurement:** **Second Order Reaction Rate Constant** in Cubic Meter per Mole Second ( $\text{m}^3/(\text{mol}\cdot\text{s})$ )  
Second Order Reaction Rate Constant Unit Conversion 



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